

Prospects of Dynamic Radius Jet Clustering Algorithm at the LHC

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Based on [JHEP 04 \(2023\) 019 \[2301.13074\]](#)

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Motivation

- High-energy colliders are crucial in advancing particle physics.
- Jets appearing from quark/gluons, are a common phenomenon in these colliders.
- High-energy machines can also produce fat jets from the boosted heavy particles.
- In-depth study of these varied objects are crucial for exploring both SM and BSM scenarios.
- However, the current fixed radius jet algorithms (kt, anti-kt, C/A) are inadequate to capture these features in a single go.
- Variable radius jet clustering algorithm would thus be an important asset in our toolbox.

Jets at Collider: QCD jets

Single colored particle gives rise to a bunch of collimated hadrons.

G. Sterman and S. Weinberg,
Phys. Rev. Lett. 39 (1977) 1436.

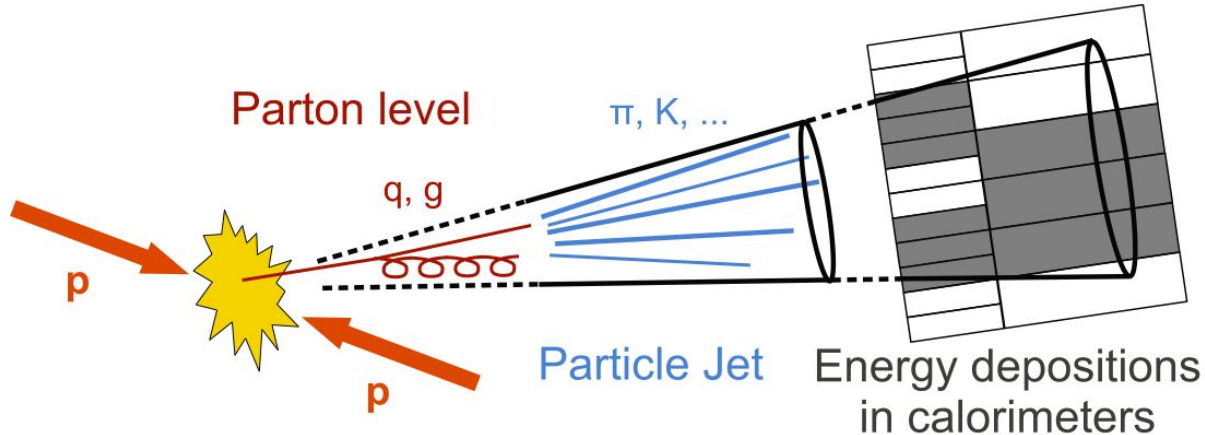
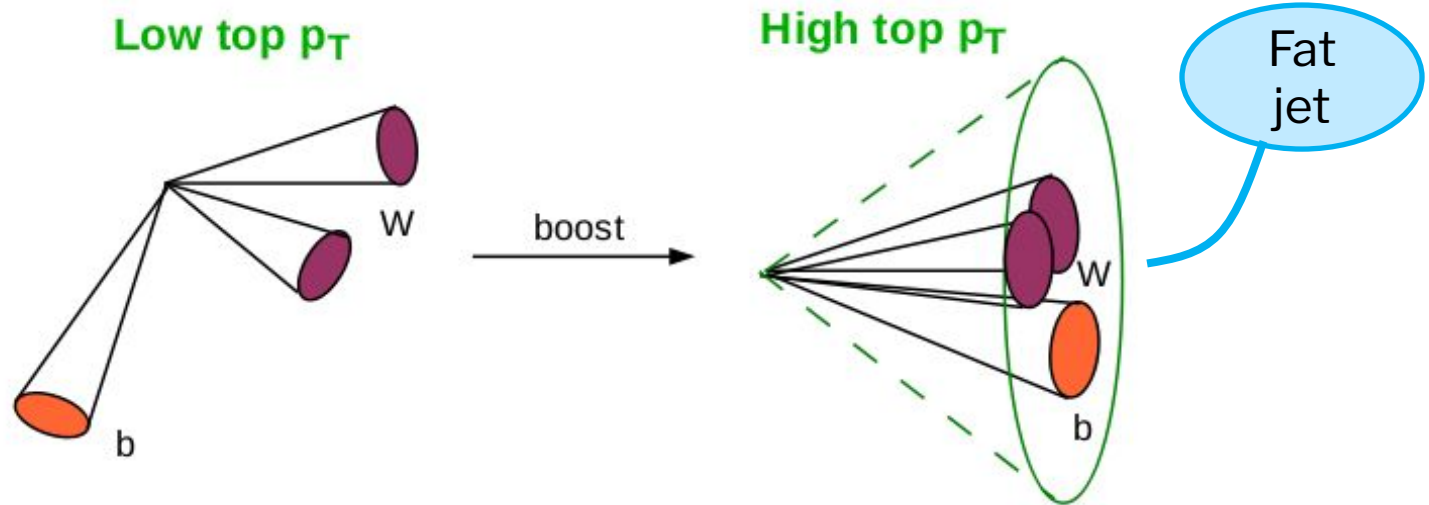


Image: [CMS.CERN](https://cms.cern)

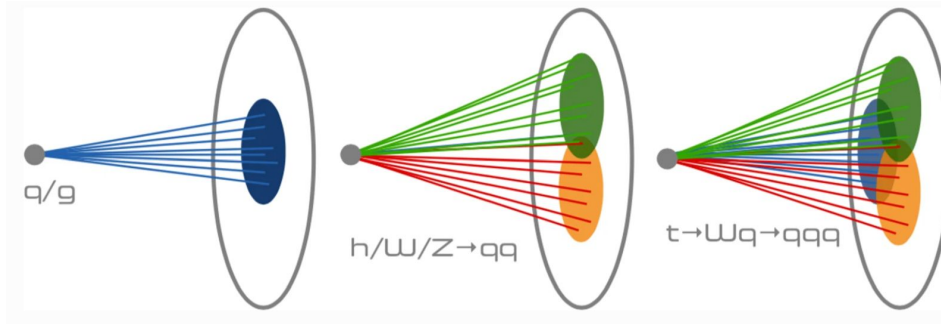
Jets at Collider: Fat jets

If a heavy particle (W, Z, top, etc.), are boosted enough, their decay products also come within a small solid angle.

These jets, called fat jets, are wider than traditional QCD jets.

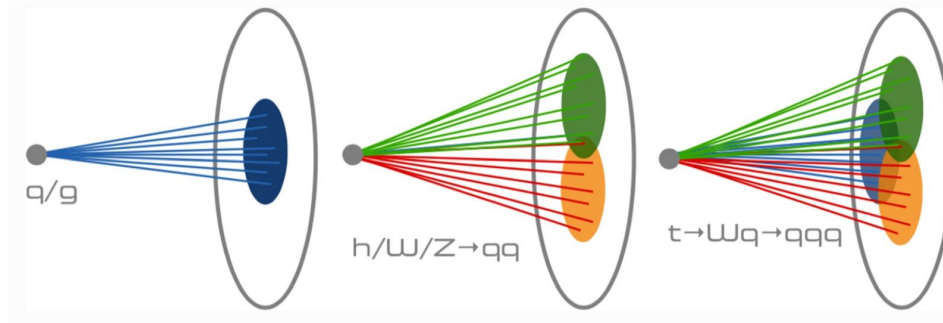


Jet Clustering Algorithm



Be it a narrow QCD jet or a boosted fat jet,
one needs an algorithm to find it by
clustering the collimated sprays of hadrons.

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Jet Clustering Algorithm

Fig: [Eur. Phys. J. C 80, 58 \(2020\)](#)

Sequential Recombination Algorithm

Take all the four-momenta in a list, calculate all possible d_{ij} and d_{iB}

$$d_{ij} = \min(p_{T_i}^{2p}, p_{T_j}^{2p}) \Delta R_{ij}^2, \quad \Delta R_{ij} = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

$$d_{iB} = p_{T_i}^{2p} R_0^2$$

p	0	1	-1
Name	CA	KT	AK

1. Find the minimum of the d_{ij} and d_{iB} .
2. Minimum is a d_{ij} : combine i , j and add to the list, remove i and j , return to step 1
3. Minimum is a d_{iB} : declare i to be a jet (final), remove it from the list, return to step 1.
4. Stop when list gets empty.

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Fixed
radius R_0

Review: [Eur. Phys. J. C 67 \(2010\) 637](#).

Dynamic Radius Jet Algorithm

$$d_{ij} = \min(p_{T_i}^{2p}, p_{T_j}^{2p}) \Delta R_{ij}^2, \quad \Delta R_{ij} = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

$$d_{iB} = p_{T_i}^{2p} (R_0 + \sigma_i)^2$$

Radius modifier

R_d^2

$$\sigma_i^2 = \frac{\sum_{a < b} p_{T_a} p_{T_b} \Delta R_{ab}^2}{\sum_{a < b} p_{T_a} p_{T_b}} - \left(\frac{\sum_{a < b} p_{T_a} p_{T_b} \Delta R_{ab}}{\sum_{a < b} p_{T_a} p_{T_b}} \right)^2; \quad a, b \in i$$

$\langle \Delta R^2 \rangle$

$\langle \Delta R \rangle^2$

p	0	1	-1
Algorithm	DR-CA	DR-KT	DR-AK

AK: [video](#).

DR-AK: [video](#).

Why σ_i ?

➤ $\sigma_i^2 = \langle \Delta R^2 \rangle - \langle \Delta R \rangle^2$
(standard deviation) measures fuzziness of a jet.

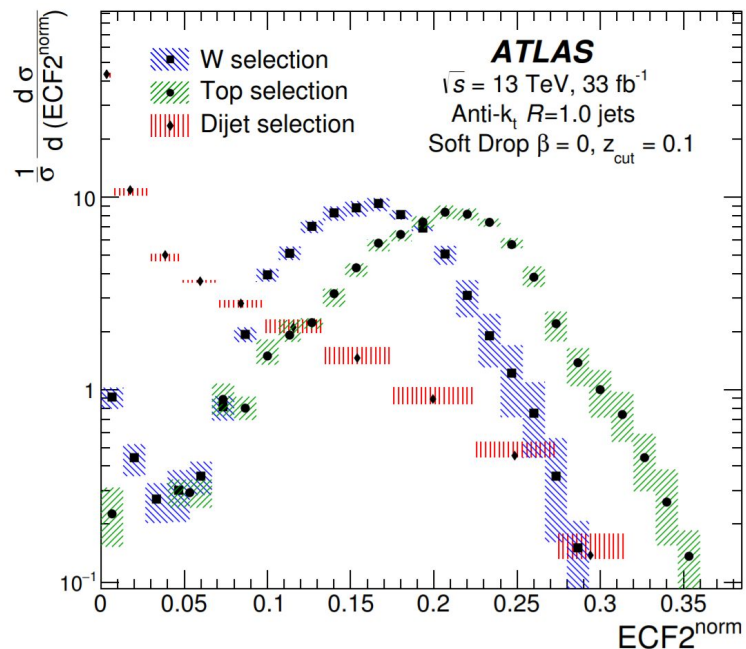
➤ Fat jets are expected to be fuzzier than QCD jets

➤ Energy Correlation Function:

$$\text{ECF2}_\beta = \sum_{a < b} p_{T_a} p_{T_b} \Delta R_{ab}^\beta$$

ECF: [JHEP 06 \(2013\) 108](#).

Fig: [JHEP 08 \(2019\) 033](#).



Implementation and tools

Implemented within the framework of **FastJet3** as a plugin.

GitHub: <https://github.com/tousiksamui/DynamicRJetAlgorithm>

$$pp \rightarrow tj$$
$$pp \rightarrow b'b' \rightarrow tW^- \bar{t}W^+$$

- Model: SARAH + SPheno
- Event generation: MadGraph5 + Pythia8

13 TeV LHC

Illustration (SM): $pp \rightarrow tj$

13 TeV LHC

$pp \rightarrow tj$

Fat jet

QCD jet

top

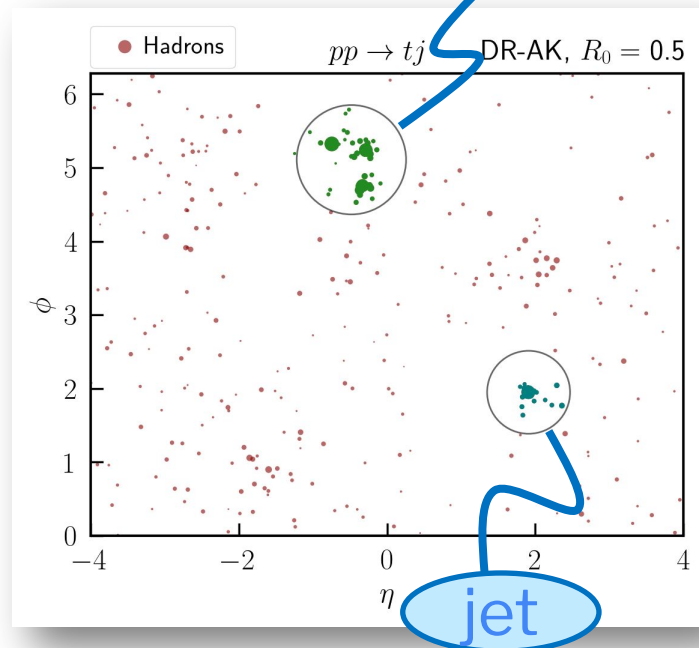
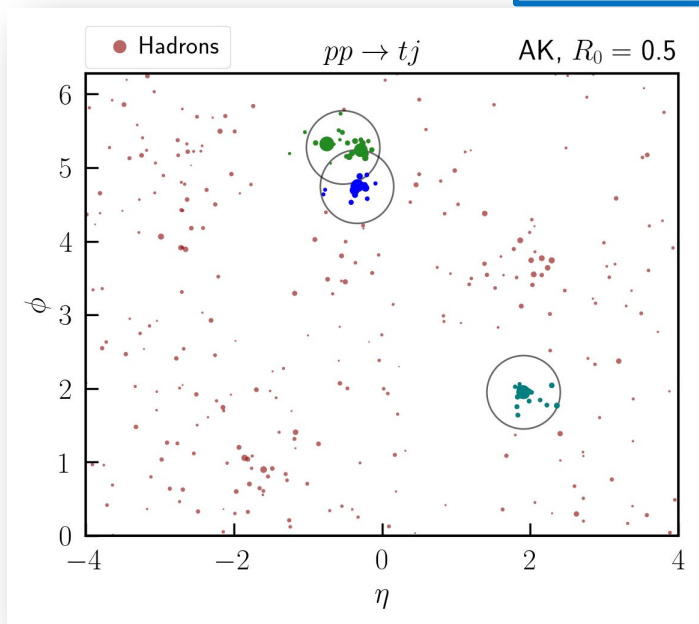


Illustration (SM): $pp \rightarrow tj$

Acceptance efficiency $\mathcal{A} = \frac{\text{No. top reconstructed events}}{\text{No. of total events}}$

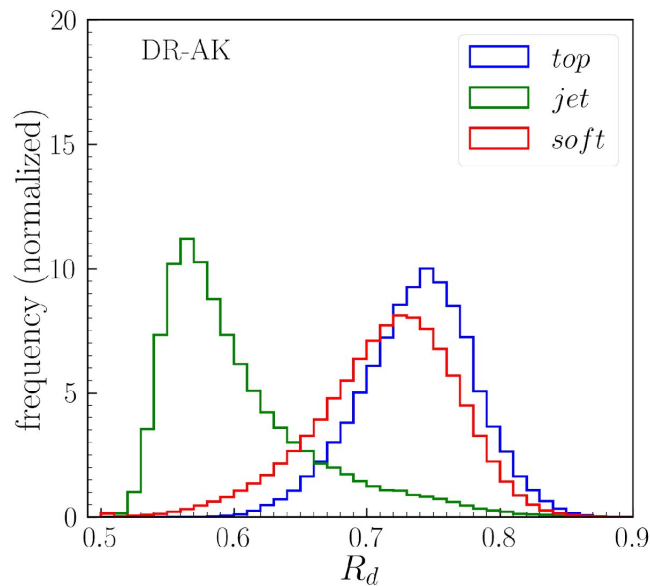
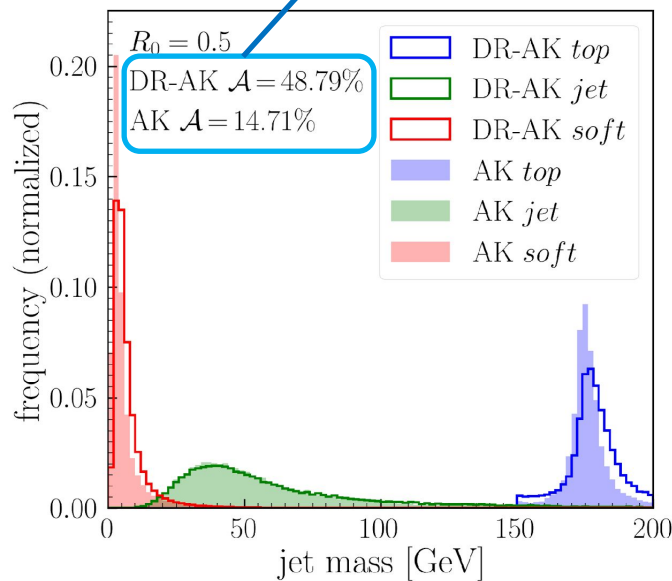
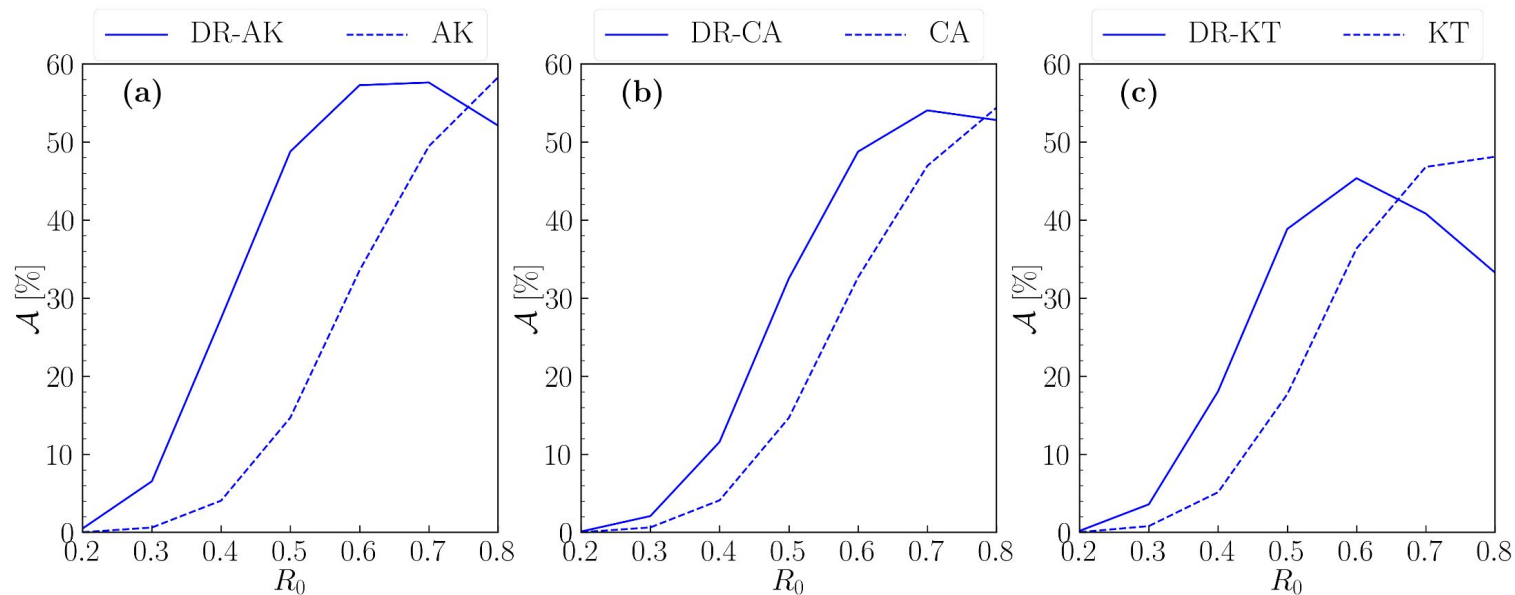


Illustration (SM): $pp \rightarrow tj$



Acceptance efficiency (\mathcal{A}) vs. initial radius (R_0)

Illustration (BSM): $pp \rightarrow b'\bar{b}' \rightarrow tWtW$

$$pp \rightarrow b'\bar{b}' \rightarrow tWtW$$

13 TeV LHC

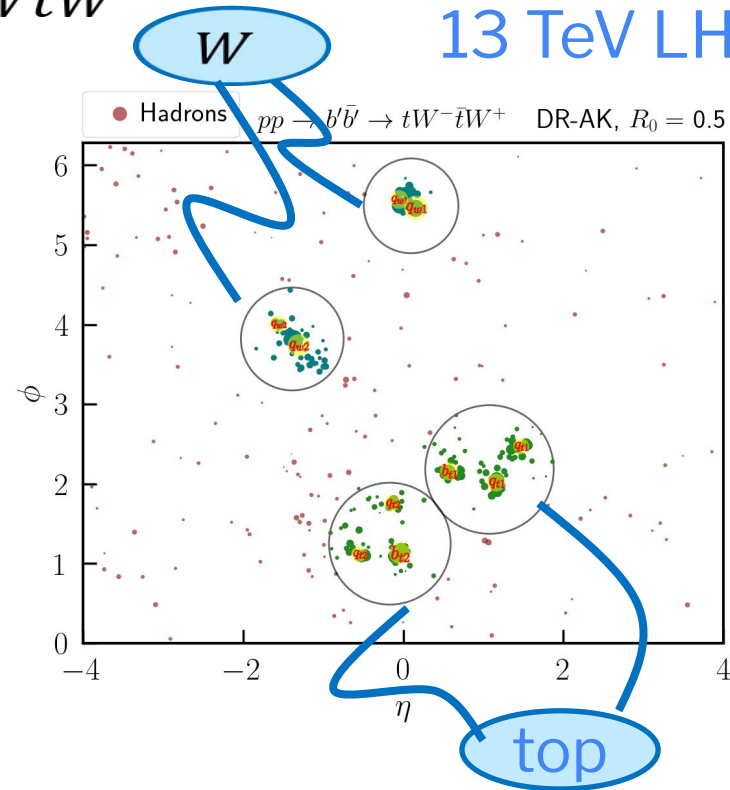
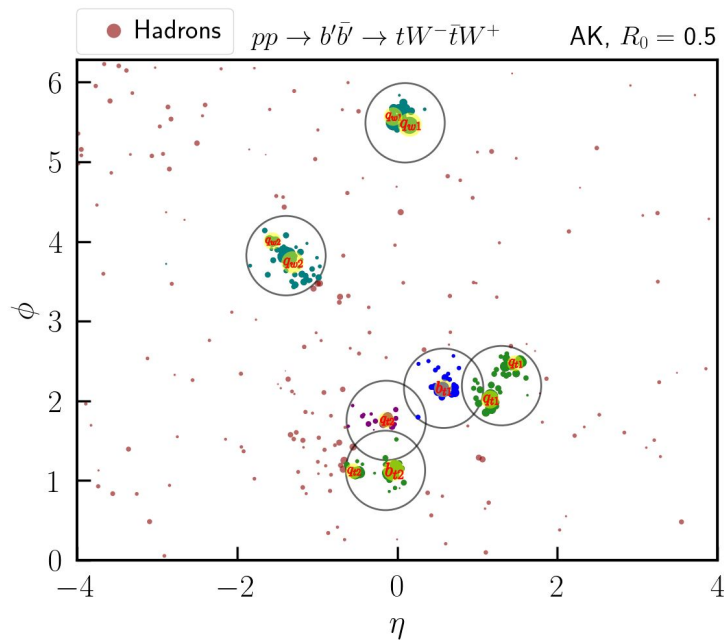
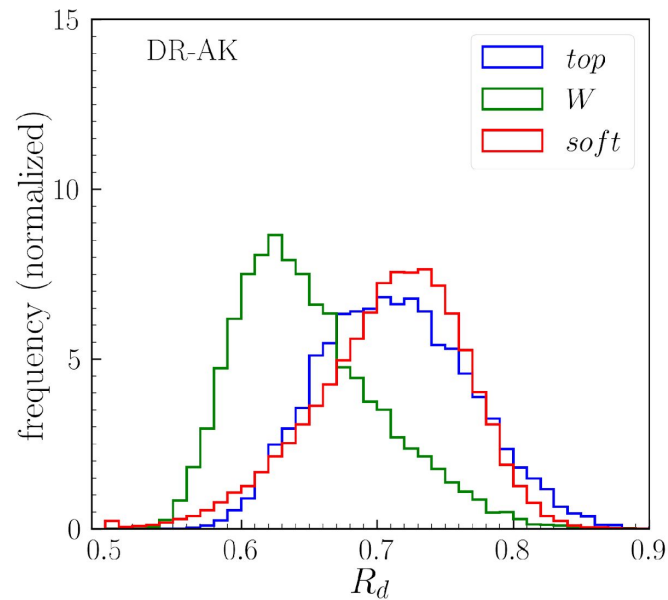
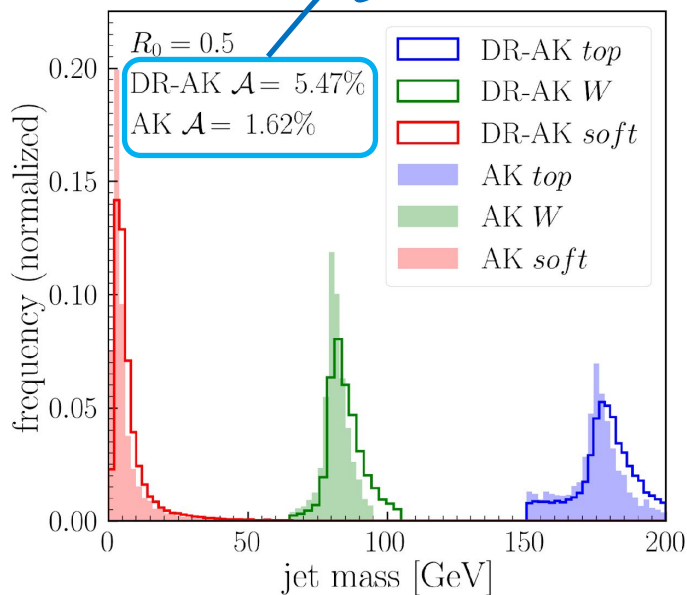


Illustration (BSM): $pp \rightarrow b'\bar{b}' \rightarrow tWtW$

Acceptance efficiency $\mathcal{A} = \frac{\text{No. top and } W \text{ reconstructed events}}{\text{No. of total events}}$



Summary

- There is a need for variable radius jet algorithm. Current fixed-radius algorithms are inadequate for this purpose.
- We have proposed a jet algorithm with dynamic radius.
- Discussed the idea, implementation this algorithm and utility
- Applicable in scenarios with differently sized jets.
- The usefulness of the DR jet algorithm has presented in two process at 13 TeV LHC.
- It has implications in the study of heavy objects (top/W/Z/H).
- Other studies related to this algorithm are ongoing.

Outlook

- Phenomenological implications especially in the BSM context has also been proposed to be studied.
- Prospects in object based studies: q/g discrimination, dark jets, W/Z/top jets.
- Prospects in theoretical, phenomenological, developmental aspects of this algorithm.
- Studies with **Open Data**:
 - A detailed study of pileup and jet energy resolution calibration (JERC) with open data has been proposed.
 - Assessing performance of the algorithm in handling boosted objects or heavy flavour jet.
 - Study of boosted objects with this new algorithm would be useful.

Thank You

